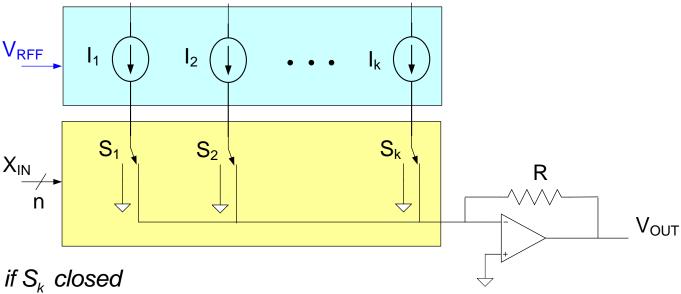
EE 505

Lecture 16



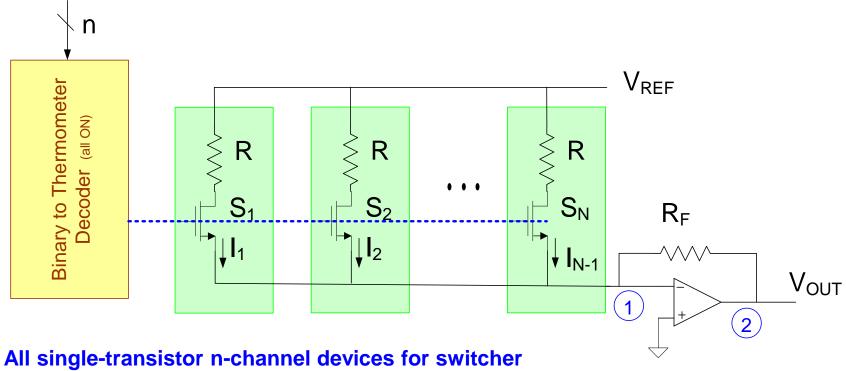




$$d_k = \begin{cases} 1 & \text{if } S_k \text{ closed} \\ 0 & \text{if } S_k \text{ open} \end{cases}$$

$$V_{OUT} = \left[\sum_{i=1}^{k} d_i I_i\right] (-R)$$

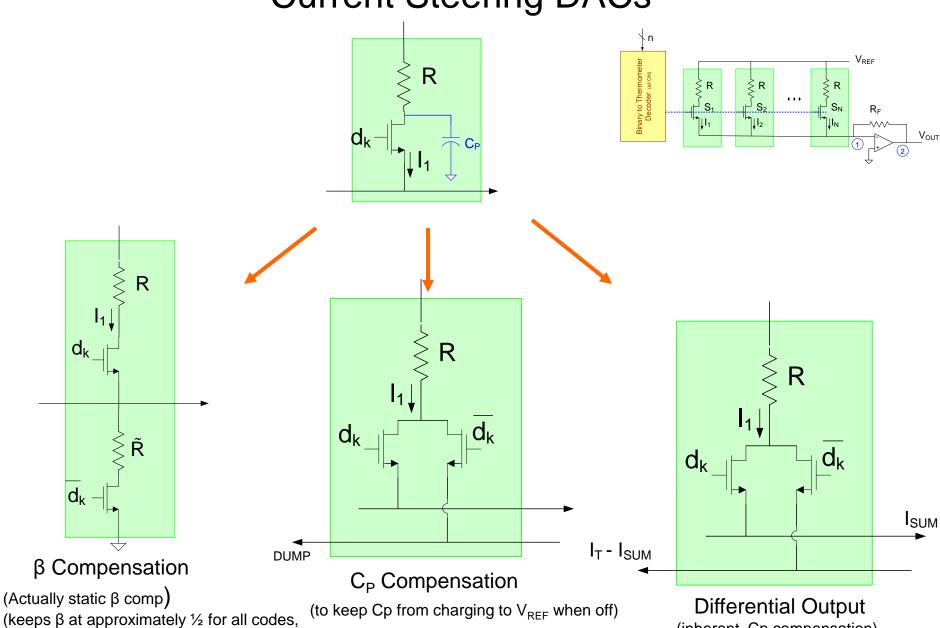
- Current sources usually unary or binary-bundled unary
- Termed bottom-plate switching
- Can eliminate resistors from DAC core
- Op Amp and resistor R can be external
- Can use all same type of switches
- Switch impedance not critical nor is switch matching
- Popular MDAC approach



- **Unary R:switch cells**
- Parasitic capacitances on drain nodes of switches cause transient settling delays
- R+Rsw is nonlinear (so nonlinear relationship between I_k and V_{REF}) but does not affect linearity of DAC
- **Resistor and switch impedance matching important**
- Previous code dependent transient (parasitic capacitances on drains of switches)

Review from Last Lecture

Current Steering DACs

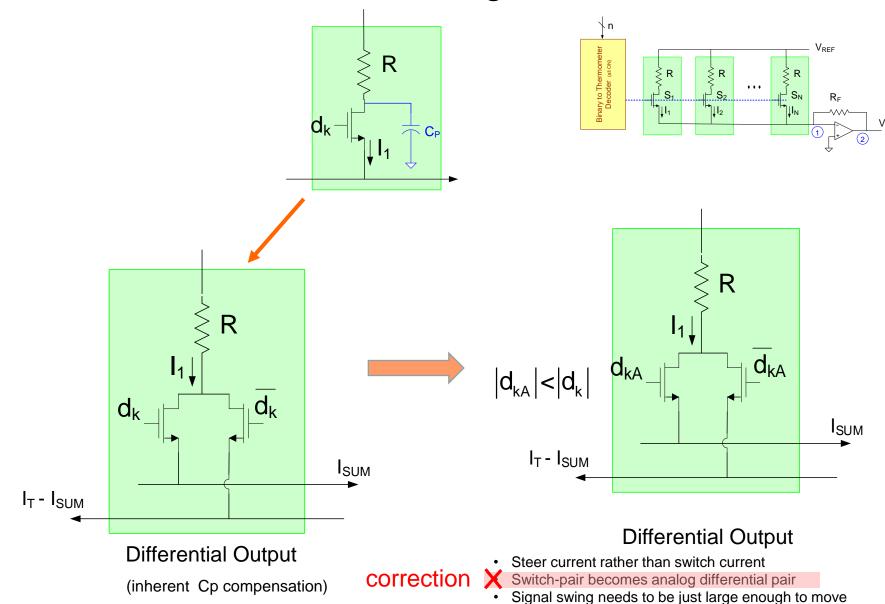


(keeps β at approximately $\frac{1}{2}$ for all codes, reduces size of compensation capacitor))

(inherent Cp compensation)

Review from Last Lecture

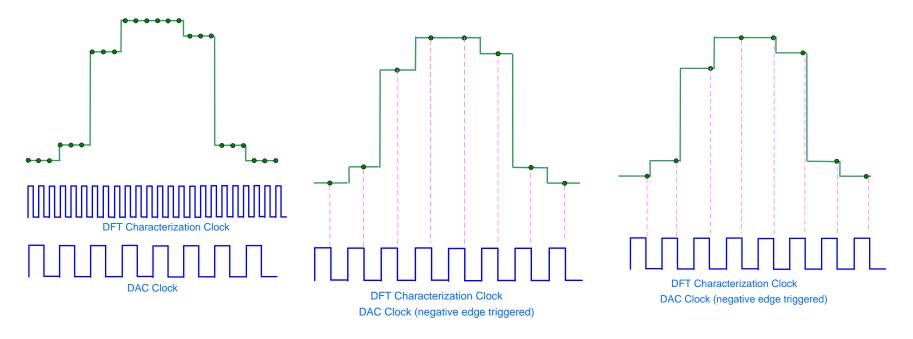
Current Steering DACs



current from left side to right side

Review from Last Lecture

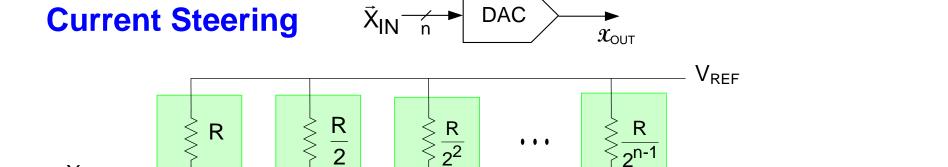
Spectral Characterization of DACs (a measure of linearity)



Assume Nyquist sampling rate is satisfied

Does it make a difference?

Yes! But depends on application which is useful



 S_3

Binary-Weighted Resistor Arrays

 I_3

Unary cells bundled to implement binary cells (so no net change in total number of cells)

 V_{OUT}

2

- Need for decoder eliminated!
- DNL may be a major problem
- INL performance about same as thermometer coded if same unit resistors used
- Sizing and layout of switches is critical

 S_2

 I_2

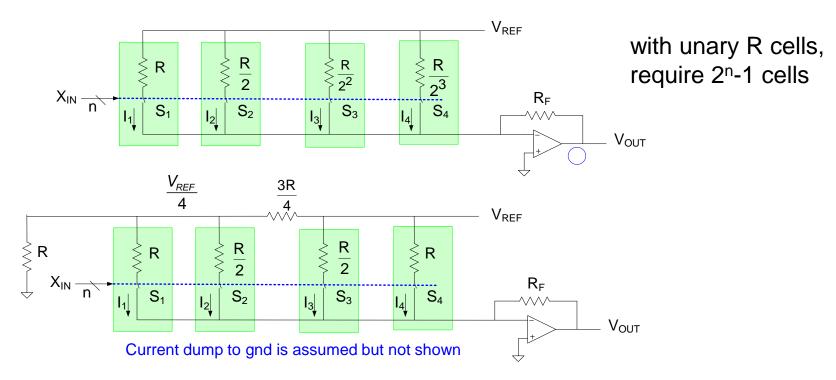
Large total resistance

Observe thermometer coding and binary weighted both offer some major advantages and some major limitations

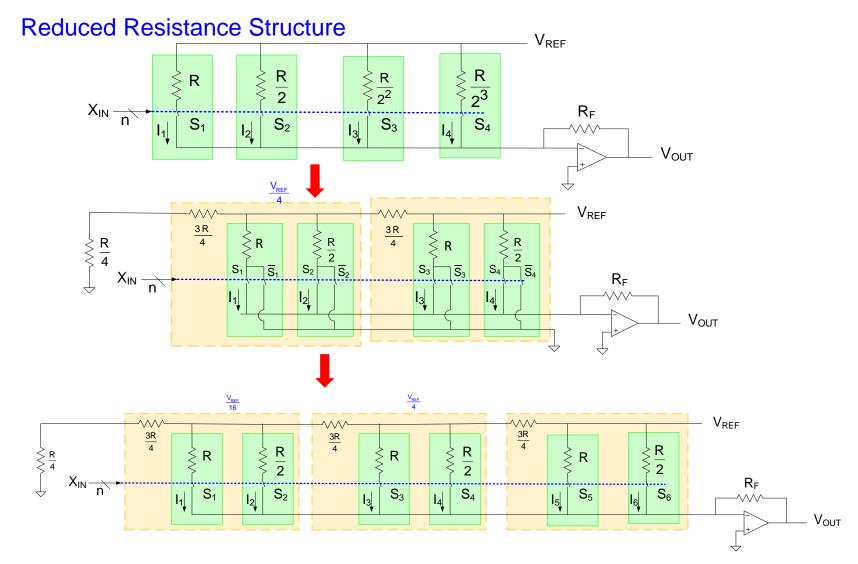
Large DNL dominantly occurs at mid-code and due to ALL resistors switching together Can unary cell bundling be regrouped to reduce DNL

Reduced Resistance Structure

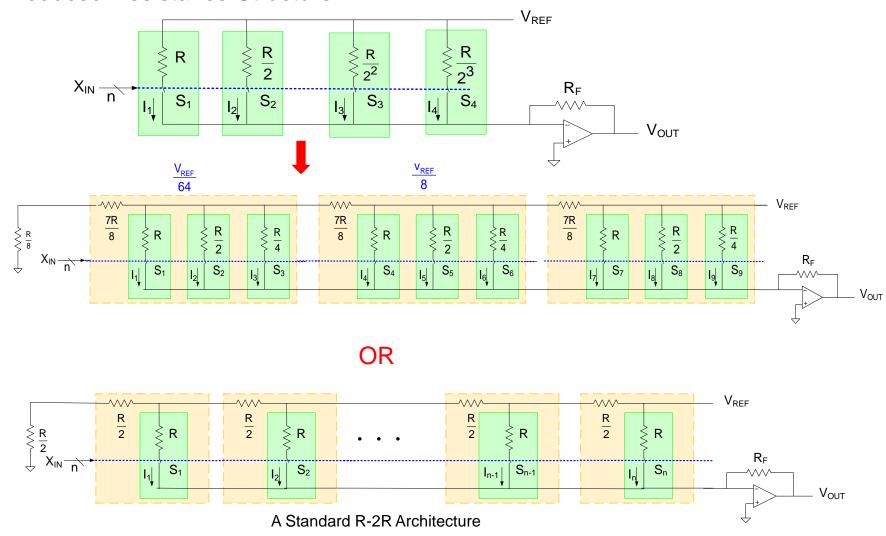
(actually concerned about number of unary cells, not total ohmic resistance)



- Significant reduction in resistance possible
- Can be inserted at more than one place to further reduce resistance values
- Introduces a "floating node" but voltage on floating node does not change (if current is stee
- Current drawn from V_{REF} does not change with code
- Dummy switching can be used for β compensation
- If inserted at each intersection becomes R-2R structure

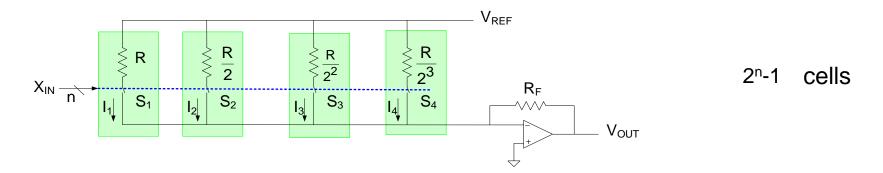


Reduced Resistance Structure

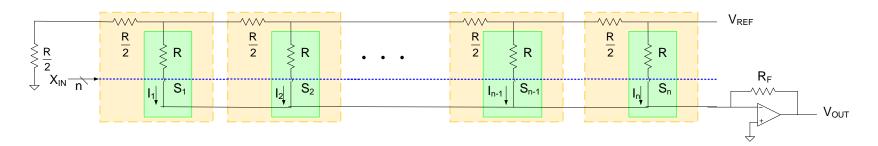


with unary R/2 cells, required 3n+1 cells compared to 2ⁿ-1 cells for binary bundled array

Reduced Resistance Structure



3n+1 cells



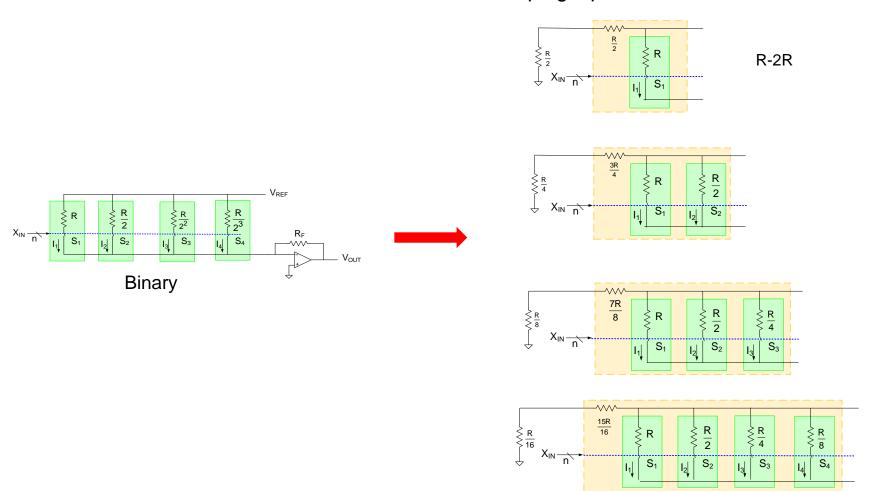
Is the R-2R structure smaller?

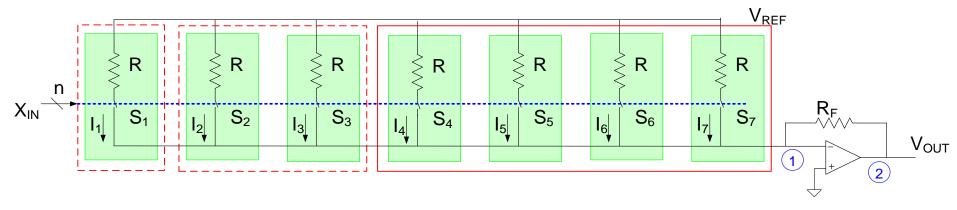
Does the R-2R structure perform better?

What metric should be used for comparing performance?

Reduced Resistance Structure

Slice Grouping Options with Series Resistors





Binary-Weighted Resistor Arrays

Actual layout of resistors is very important

Performance of Thermometer Coded vs Binary Coded DACs

Conventional Wisdom:

- Thermometer-coded structures have inherently small DNL
- Binary coded structures can have large DNL
- INL of both structures is comparable for same total area

- Will consider String DAC but nearly same results for current-steering DACs
- Current Steering DAC will generate current from resistors
- ➤ For Binary Coded DAC, MSB: 2ⁿ⁻¹ unary cells in parallel LSB: single unary cell

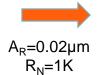
- Consider unit resistor of area 2µm² (shape not critical)
- Matching parameter A_R=0.02μm
- R_N=1K (not critical)

$$\sigma_R = \frac{R_N}{\sqrt{A}} A_{\rho R}$$

Assume Gaussian Distribution of Resistors

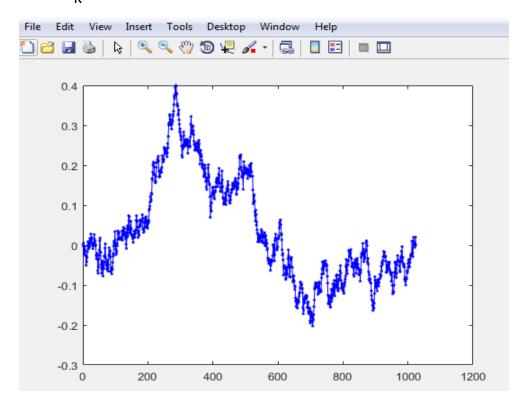
Example: n=10

String DAC



Resistor Sigma= 14.14Ω

Simulation 1: INL_k



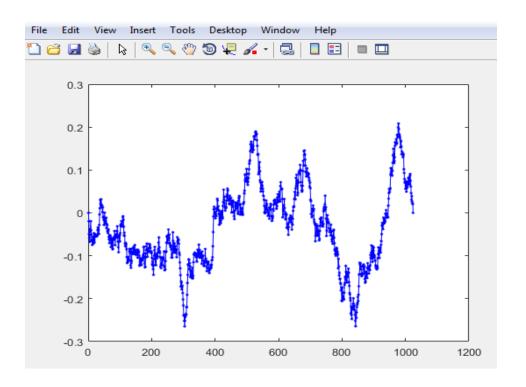
Example: n=10

String DAC



Resistor Sigma= 14.14Ω

Simulation 2: INL_k



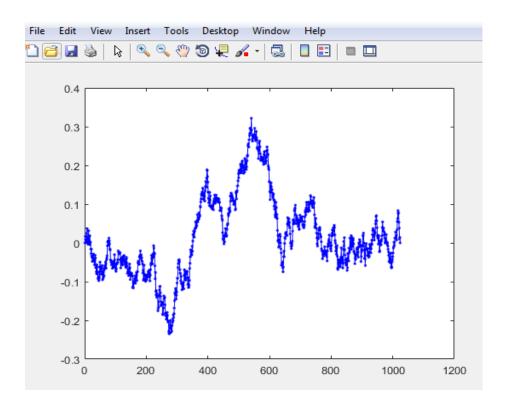
Example: n=10

String DAC



Resistor Sigma= 14.14Ω

Simulation 3: INL_k



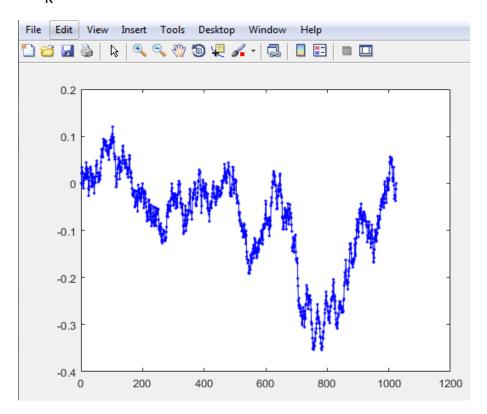
Example: n=10

String DAC



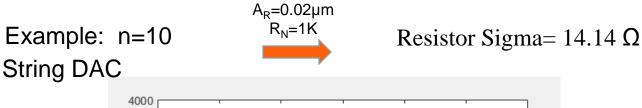
Resistor Sigma= 14.14Ω

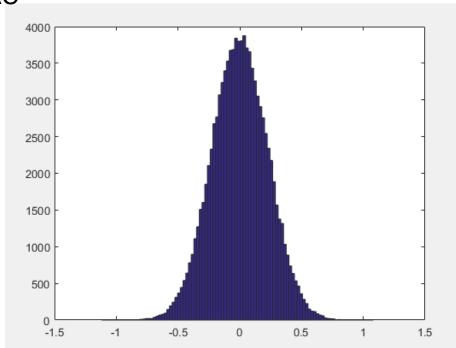
Simulation 4: INL_k





Low DNL and random walk nature should be apparent

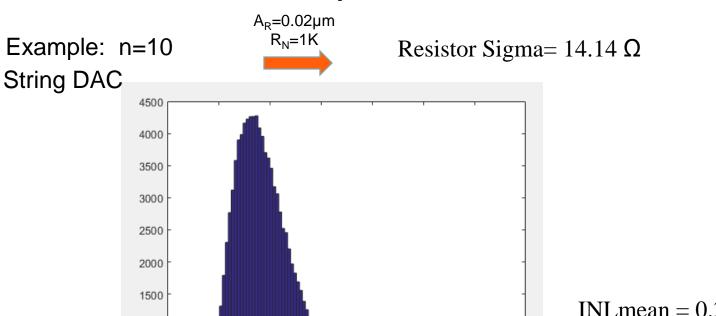




INLkmax_mean = -2.11116e-05 INLkmax_sigma = 0.226783

Histogram of INL_{kmax} from 100,000 runs

Appears to be Gaussian



INLmean = 0.384382 INLsigma = 0.117732

Histogram of INL from 100,000 runs

0.6

8.0

1.2

1.4

Not Gaussian

0.4

1000

500

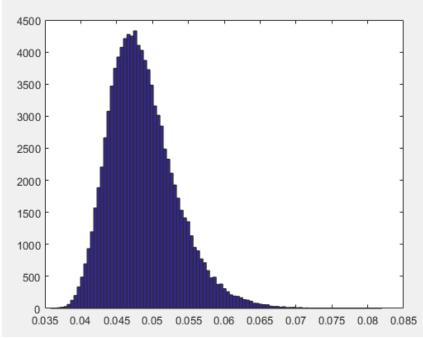
0.2

Example: n=10

 $A_R=0.02\mu m$ $R_N=1K$

Resistor Sigma= 14.14Ω

String DAC



DNLmean = 0.0486494 DNLsigma = 0.00471025

Histogram of DNL from 100,000 runs

Not Gaussian but both mean and sigma are very small

Example: n=10

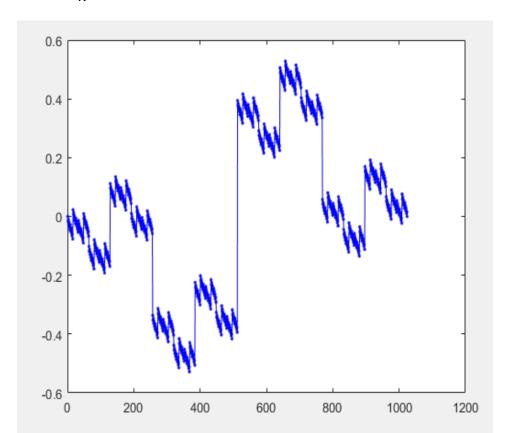
A =0.02um

Resistor Sigma= 14.14Ω

Binary DAC

A_R=0.02μm R_N=1K

Simulation 1: INL_k



Example: n=10

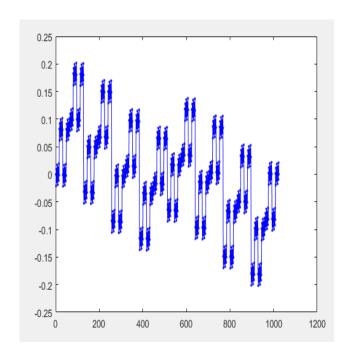
A_R=0.02μm

 $R_N=1K$

Resistor Sigma= 14.14Ω

Binary DAC

Simulation 2: INL_k



Example: n=10

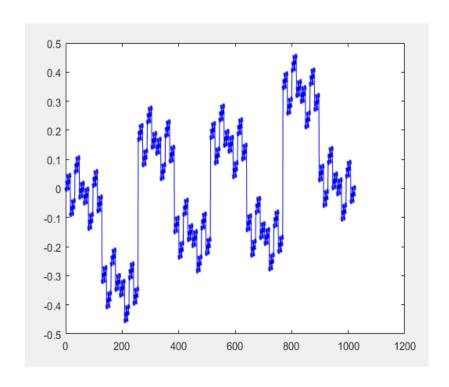
A_R=0.02μm

 $R_N=1K$

Resistor Sigma= 14.14Ω

Binary DAC

Simulation 3: INL_k



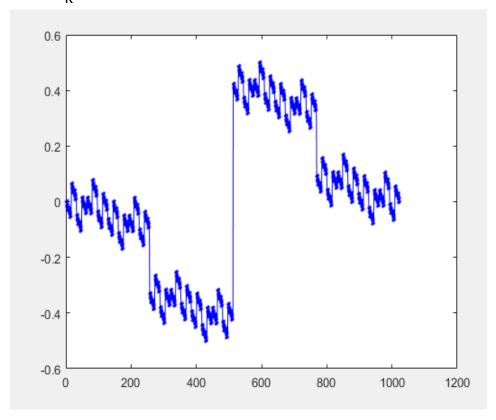
Example: n=10

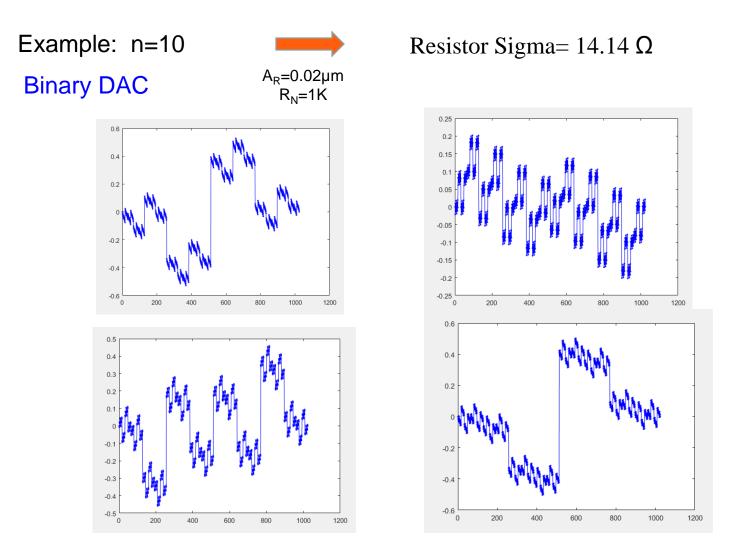
Resistor Sigma= 14.14Ω

Binary DAC

 $A_R=0.02\mu m$ $R_N=1K$

Simulation 4: INL_k





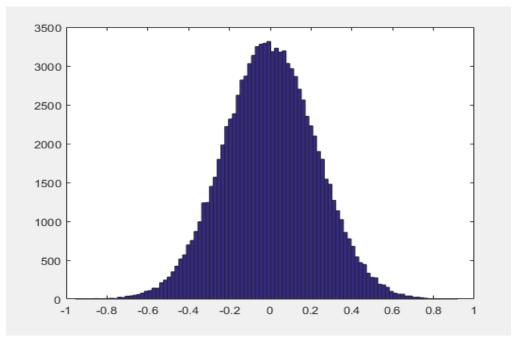
Large DNL bit INL does not appear to be much different than for string DAC

Example: n=10

 $A_R=0.02\mu m$ $R_N=1K$

Resistor Sigma= 14.14Ω

Binary DAC



INLkmax_mean = -.00526008 INLkmax_sigma = 0.23196

Histogram of INL_{kmax} from 100,000 runs

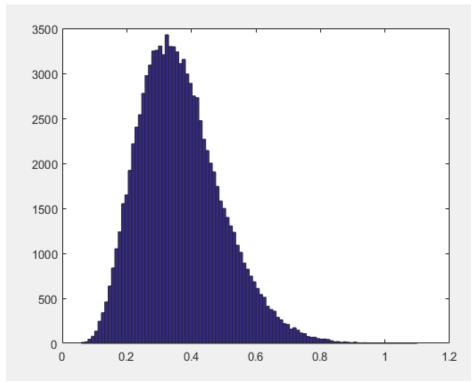
Appears to be Gaussian

Example: n=10

 $A_R=0.02\mu m$ $R_N=1K$

Resistor Sigma= 14.14Ω

Binary DAC



INLmean = 0.368441INLsigma = 0.126133

Histogram of INL from 100,000 runs

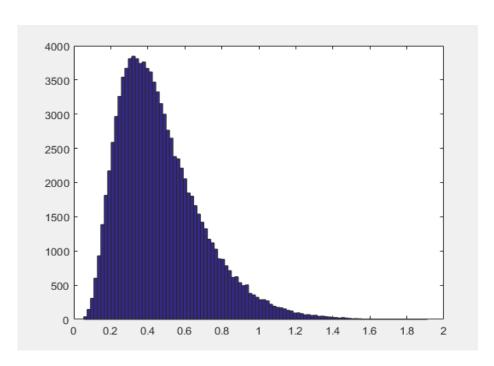
Not Gaussian

Example: n=10

Binary DAC



Resistor Sigma= 14.14Ω



DNLmean = 0.46978 DNLsigma = 0.227768

Histogram of DNL from 100,000 runs

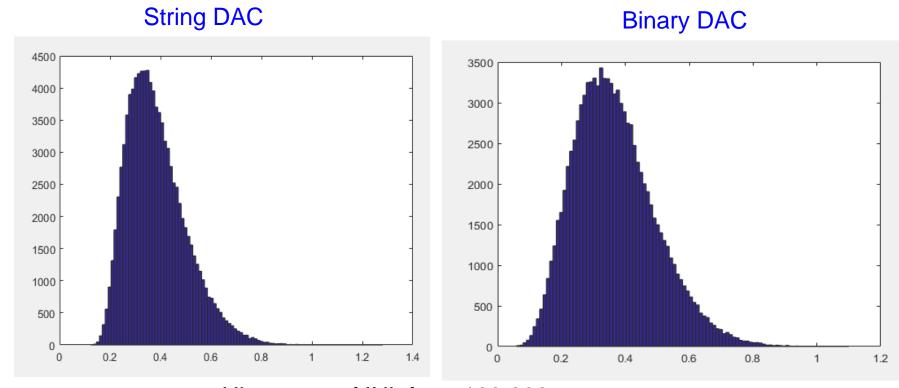
Not Gaussian and both mean and sigma are not small

Example: n=10



Resistor Sigma= 14.14Ω

Both structures have essentially the same area



Histogram of INL from 100,000 runs

Since mathematical form for PDF is not available, not easy to analytically calculate yield

Example: n=10

$$A_R=0.02\mu m$$
 $R_N=1K$

Resistor Sigma= 14.14Ω

Both structures have essentially the same area

String DAC

Resolution = 10 AR = 0.02

Rnom = 1000 Area Unit Resistor = $2\mu m^2$

INLkmax mean = -2.11116e-05

INLmean € 0.384382

INLtarget = 0.5000

Nruns = 100000

Resistor Sigma= 14.1421

INLkmax sigma = 0.226783

INLsigma = 0.117732

Yield(%) = 84.0120

Binary DAC

Resolution = 10 AR = 0.02

Rnom = 1000 Area unit resistor= $2\mu m^2$

INLmean (0.367036)

INLkmax mean = 0.000130823

 $\frac{DNLmean}{DNLtarget} = 0.46978$ $\frac{DNLtarget}{DNLtarget} = 0.5000$

Nruns = 100,000

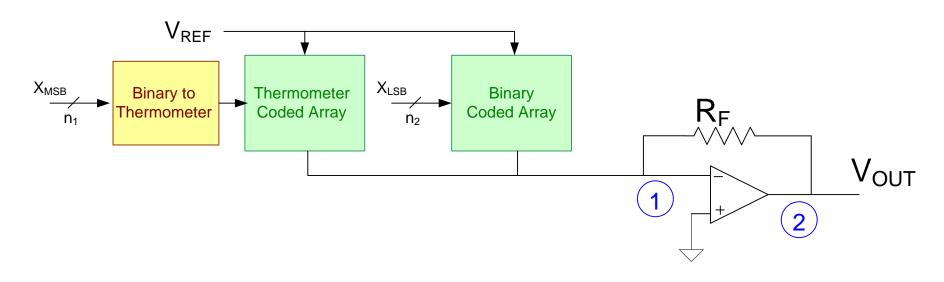
Resistor Sigma= 14.1421

INLsigma = 0.128294

INLkmax sigma = 0.226276

DNLsigma = 0.227768

Yield (%) = 84.8580

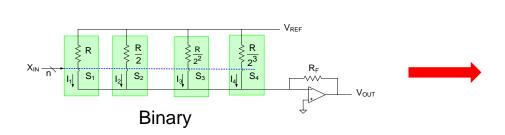


Segmented Resistor Arrays

- Combines two types of architectures
- Can inherit advantages of both thermometer and binary approach
- Minimizes limitations of both thermometer and binary approach

Reduced Resistance Structure

Slice Grouping Options with Series Resistors

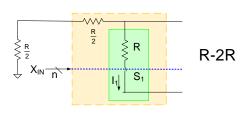


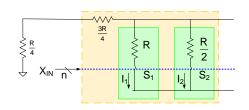
Is it better to use series unary cells to form R or parallel unary cells to form $\frac{R}{2^n}$?

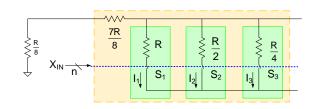
In the two scenarios, is the dominant area allocated to the MSB or the LSB part of the ladder?

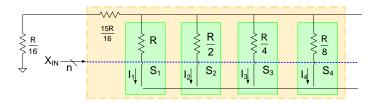
Will this choice make much difference in yield?

What yield-related performance metric will be most affected?



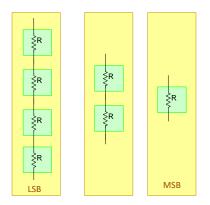


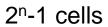


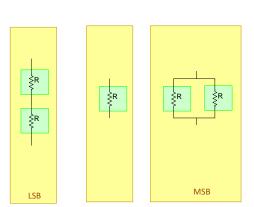


Reduced Resistance Structure

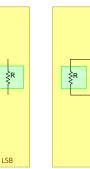
Is it better to use series unary cells to form R or parallel unary cells to form $\frac{R}{2^n}$?



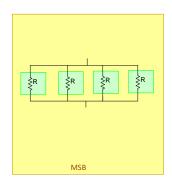




for n odd $2^{\frac{n+3}{2}} - 3$ cells



R



2ⁿ-1 cells

n	Series	Parallel	Split
3	7	7	5
5	31	31	13
7	127	127	29
9	511	511	61
11	2047	2047	125
13	8191	8191	253
15	32767	32767	509

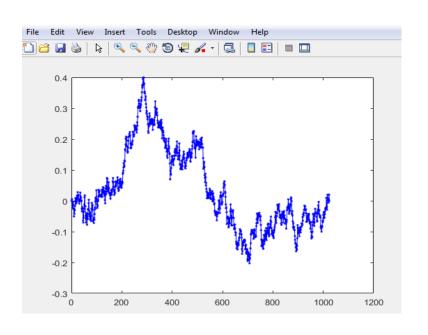
Example: n=10

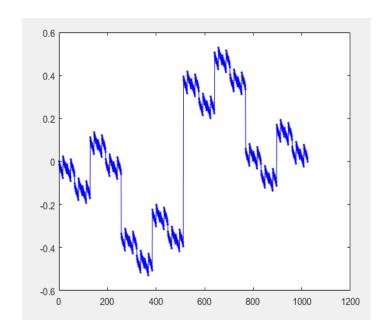
String DAC



Resistor Sigma= 14.14Ω

Simulation 1: INL_k





String

Binary Weighted

Actual outputs will differ significantly



Stay Safe and Stay Healthy!

End of Lecture 16